

Numerical Simulation of Turbulent Boundary-Layer Flows... ...using Ekman



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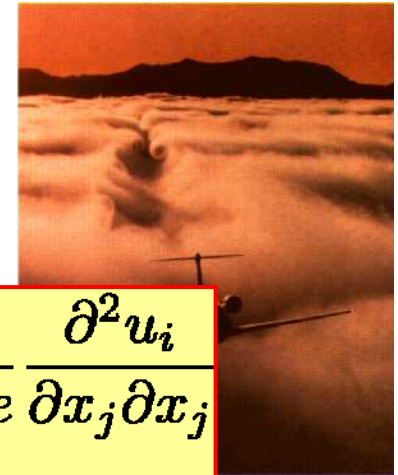
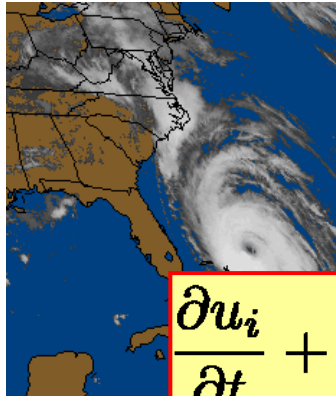


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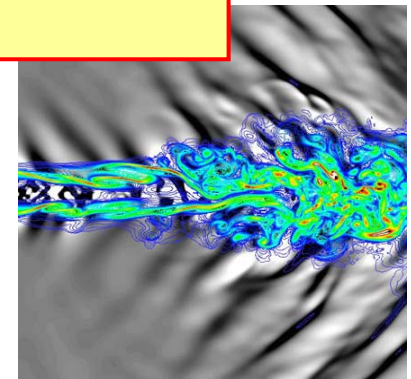
Turbulent flows are everywhere, and they can be described by ...



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$$\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{1}{Re} \frac{\partial^2 u_i}{\partial x_j \partial x_j}$$
$$\frac{\partial u_i}{\partial x_i} = 0$$

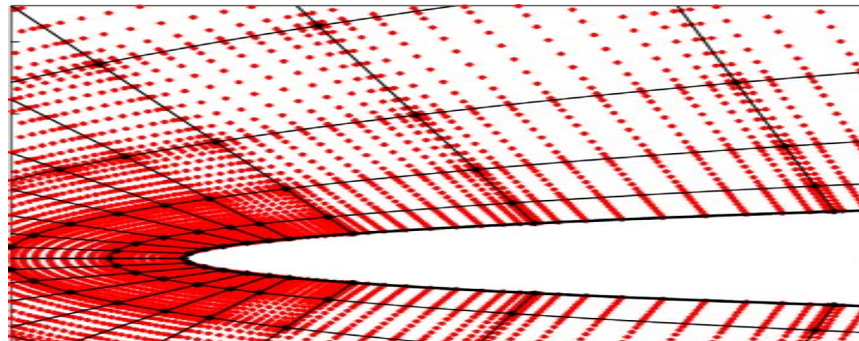


How do we perform numerical experiments?

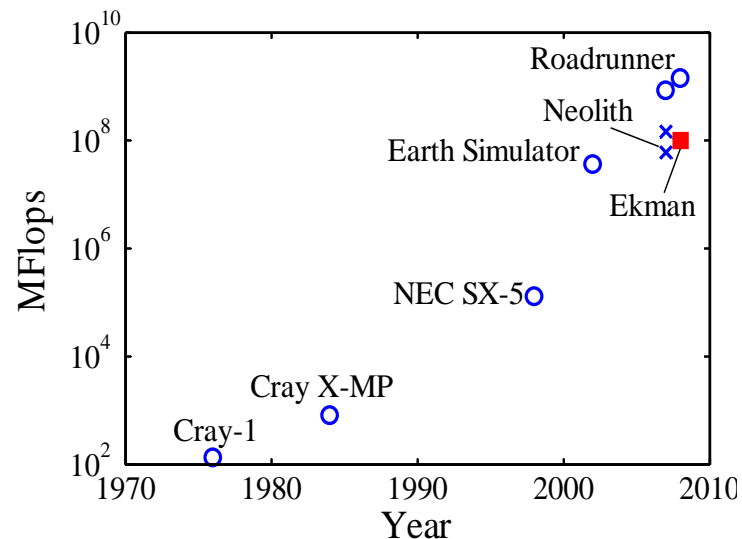
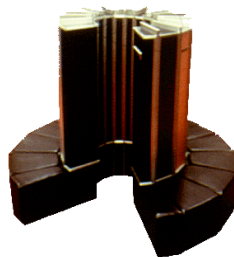
- Solve the Navier-Stokes equations for the velocity on grid points using super computers



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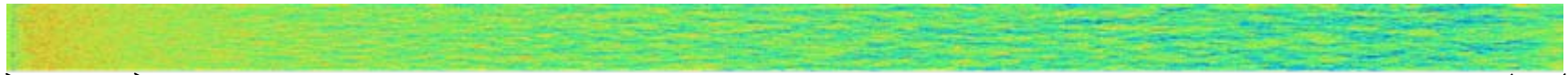


Cray-1 (1976)
100 Mflops
1 processor



Ekman Dell cluster
(2008) 70 Tflops
10000 processors

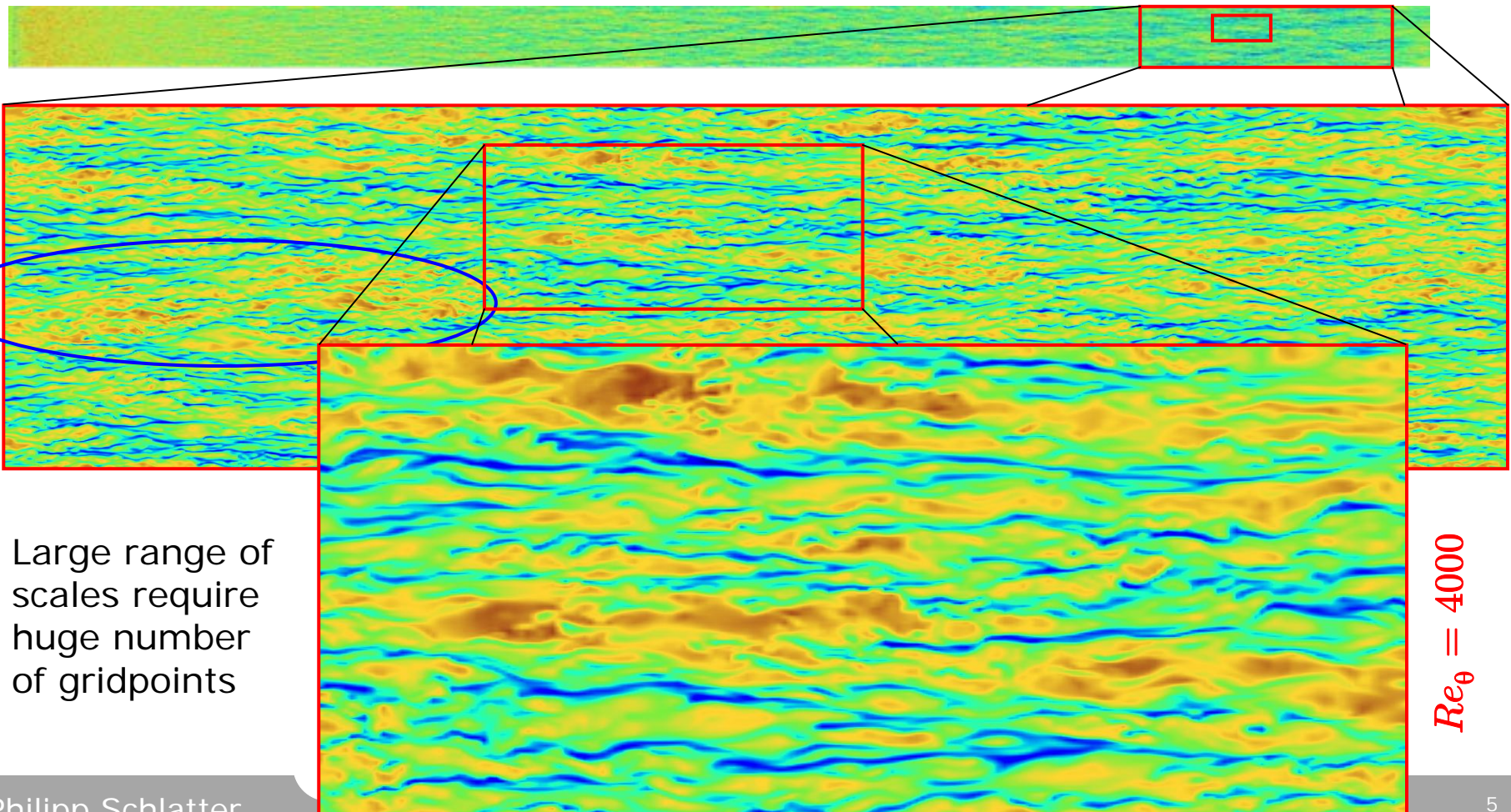
Numerical simulations turbulent flow close to solid walls...



Turbulence close to the surface →
Friction → Drag → Fuel consumption

Numerical simulations of turbulent flow

- DNS with $8192 \times 513 \times 768 = 7.5$ billion grid points running on 4096 cores



How can simulations help make modern aircraft more environmentally friendly?



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- Suppressing turbulence on the wings (laminar flow control) improve fuel efficiency
- Better models of turbulence on wing surfaces improve engineering design
- Example: Airbus green aircraft concept



EU NACRE project:
Concept for quiet, light
fuel efficient aircraft

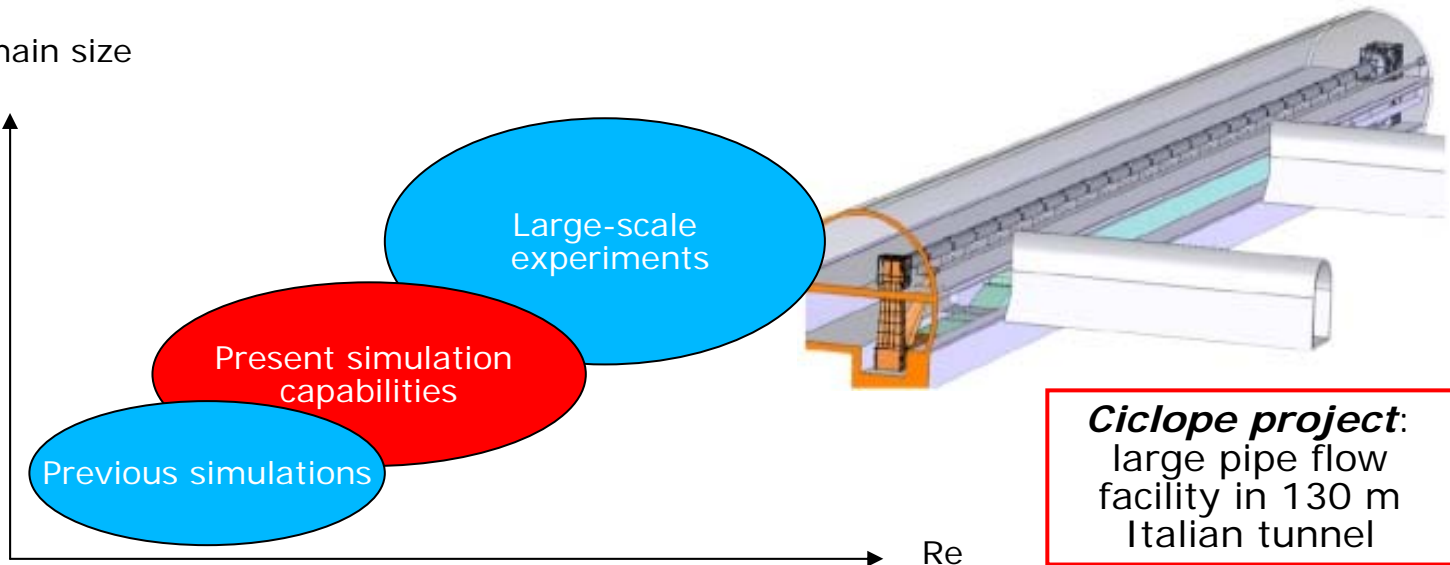
What can we learn from even larger simulations?

- $8192 \times 513 \times 768 = 7.5$ billion grid points
- Overlap with large-scale experiments



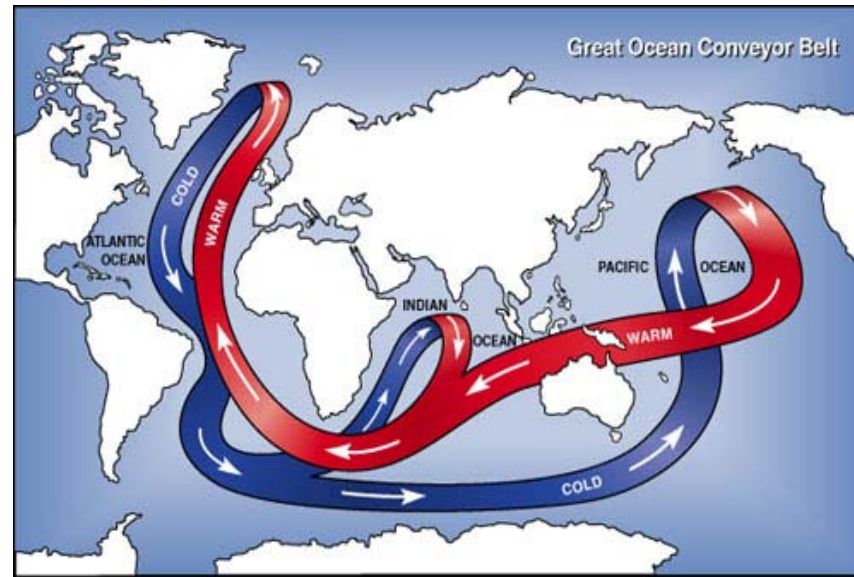
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Domain size



Measurement jamboree
(Marusic, Nagib, Smits, Alfredsson...)

How will the ocean circulation respond to global warming?



- Ocean large heat regulator of climate
- Great conveyor belt transport warm surface water to north pole and cold water back along bottom
- Circulation affected by global warming?



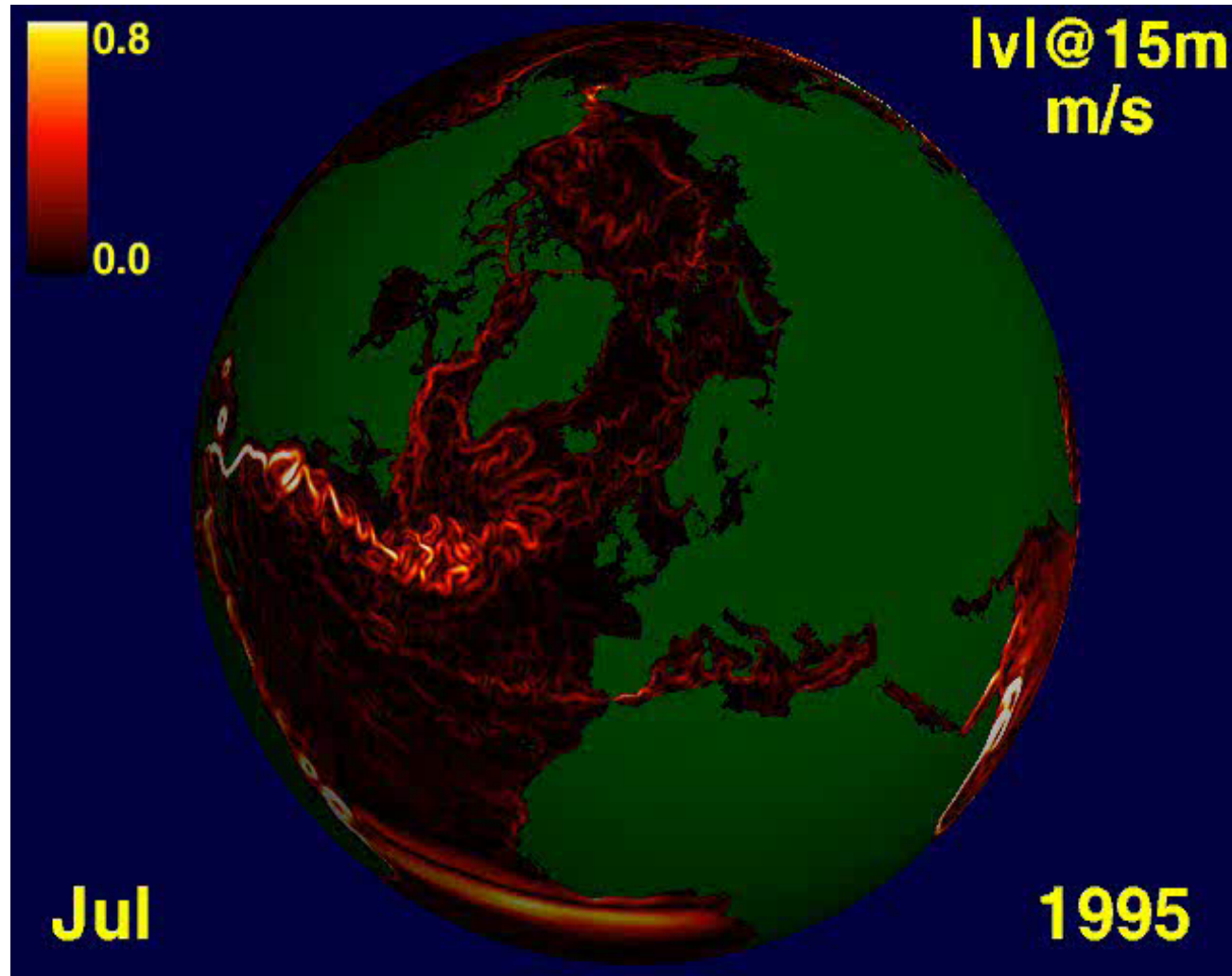
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The ocean is turbulent!



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Simulation: ECCO
code using MITgcm.
JPL. NASA Ames

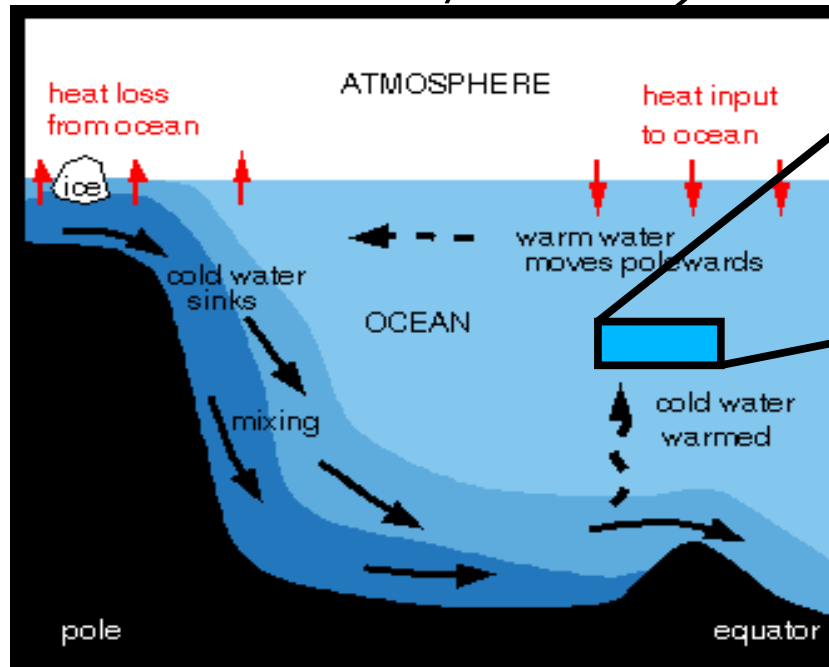


The global circulation is very sensitive to the turbulent diffusivity

(Nilsson *et al.*, MISU)



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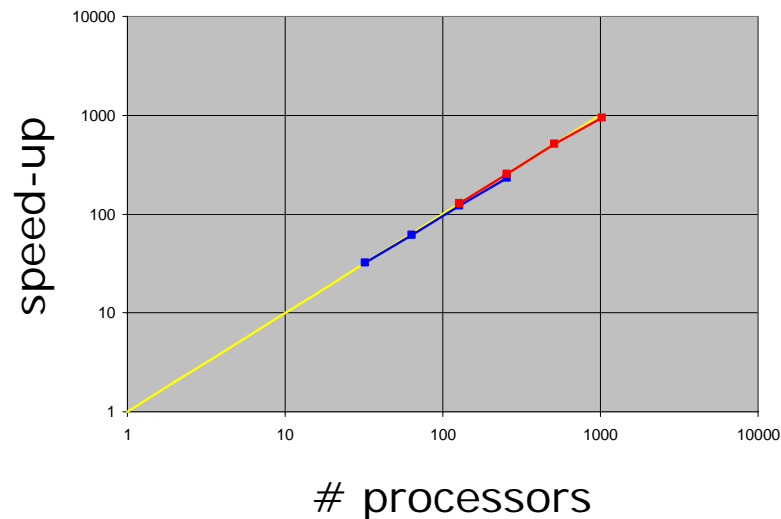
There is even turbulence at centimeter scale!

Smaller scales determine turbulent diffusivity, how fast is the cold water cooling the warmer water above ?

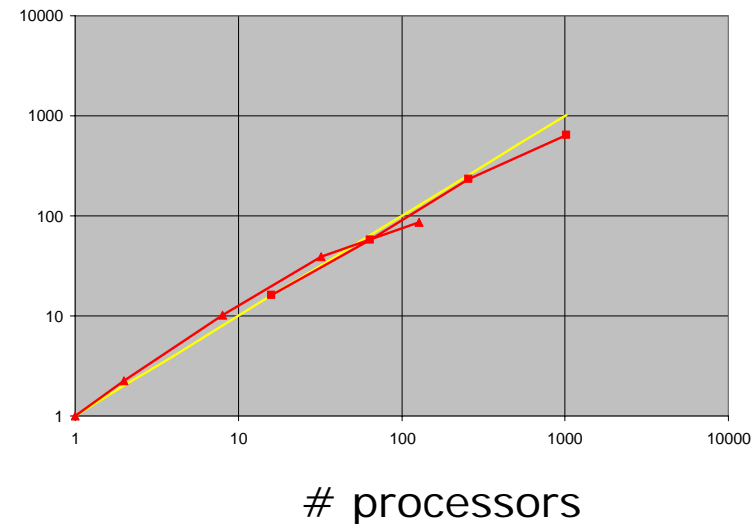
Efficient simulations on many processors



Nek5000 (spectral element)



SIMSON (fully spectral)



How much faster does the simulation run on many processors?

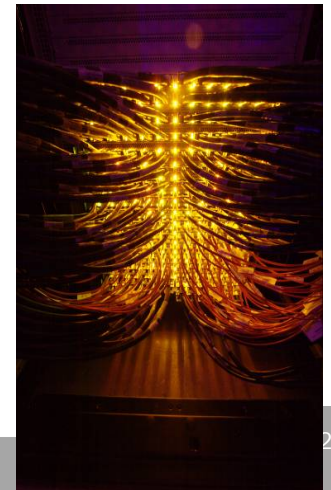
— linear scaling —●— measurements (IBM BG/L)

from 256 to 4096 cores: 85% parallel efficiency!

Ekman / Vagn

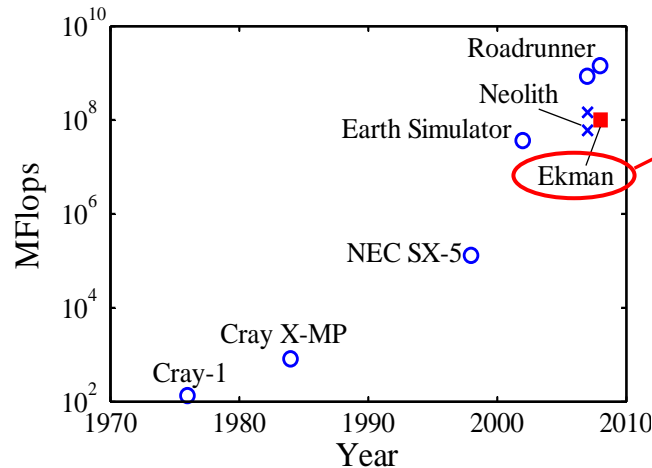


- **New supercomputer entirely dedicated for research on turbulence and climate!**
Sponsors: Wallenberg foundation and SNIC
- **Status:** **Ekman**/PDC (1268 nodes → 10144 cores → 70TFlops) and **Vagn**/NSC in production use by groups at KTH Mechanics, MISU, and SMHI.
- **Ekman:** Compilers, MPI, queue system and file system (~100TB) installed and in full usage.
- **Vagn:** 6 analysis nodes, GPFS ready, final size ~500TB with tape robot, acquiring in phases.
- **Policy:**
Large jobs/projects are prioritised.
"Ekman group" is deciding on priorities
Code performance shall be monitored



Fotograf: Harald Barth, PDC

Where does that put us...?



~ 100 times smaller than largest systems (about place 75 in top500)

→ possibility to run much larger jobs than previously possible!



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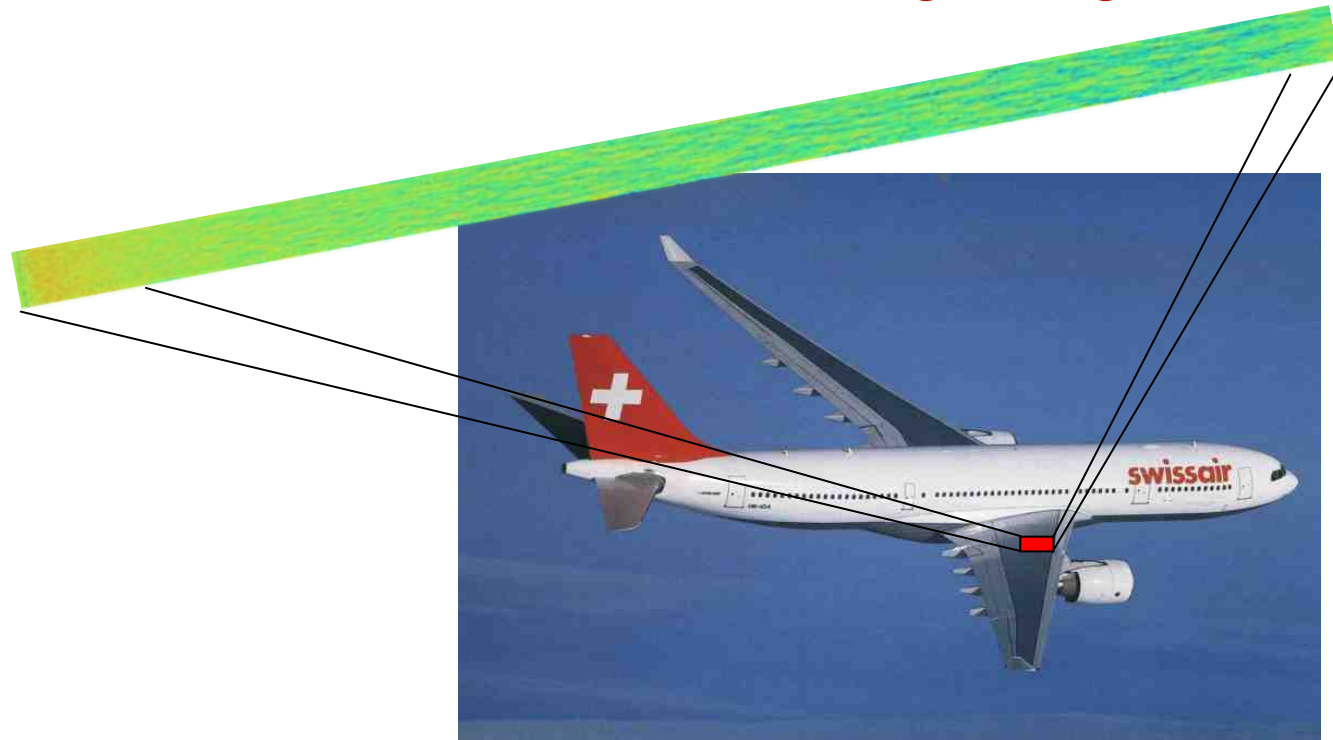
HOWEVER:

- Other groups (e.g. USA, Japan, Germany) are also heavily investing. **Routine usage** of e.g. large BG/P with $O(50'000)$ cores.
- Ekman is a **complement** to enable **very large jobs** featuring a **special mix of jobs** (width and length), and not a "normal" SNIC machine.

FOCUS: Turbulent Boundary Layer



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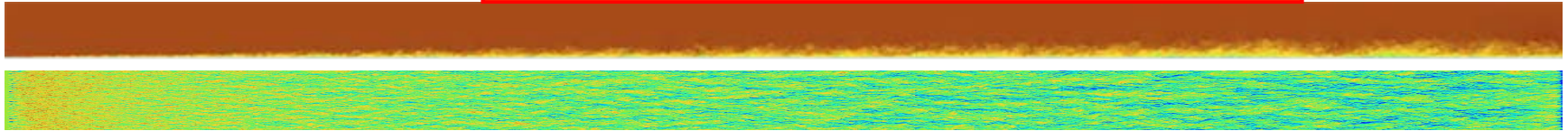
WHY?

- many (fundamental) open questions
- engineering importance (drag!)
- very timely, both experiments and simulations

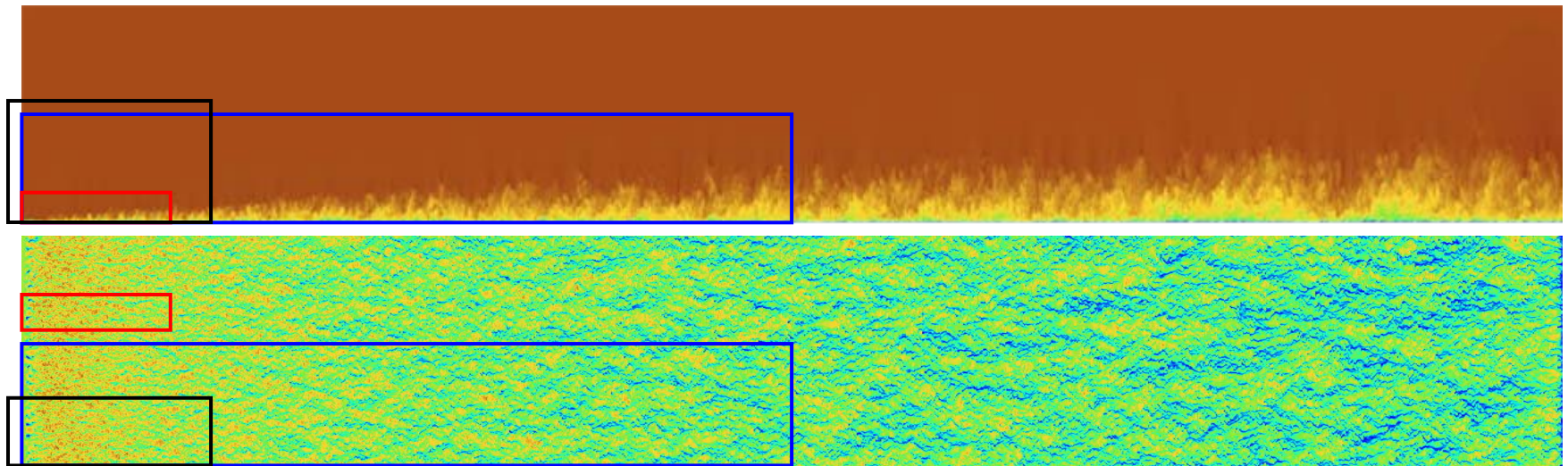
TBL up to $Re_\theta = 4000$

real aspect ratio:

$O(10^{10})$ grid points, 4096 processors



aspect ratio 4:1 :



$Re_\theta=180$

$Re_\theta=1000$

$Re_\theta=1410$

$Re_\theta=2500$

$Re_\theta=3500$

$Re_\theta=4000$

Box "medium/fine DNS"

Box Skote (2001) Box Wu&Moin (2009)

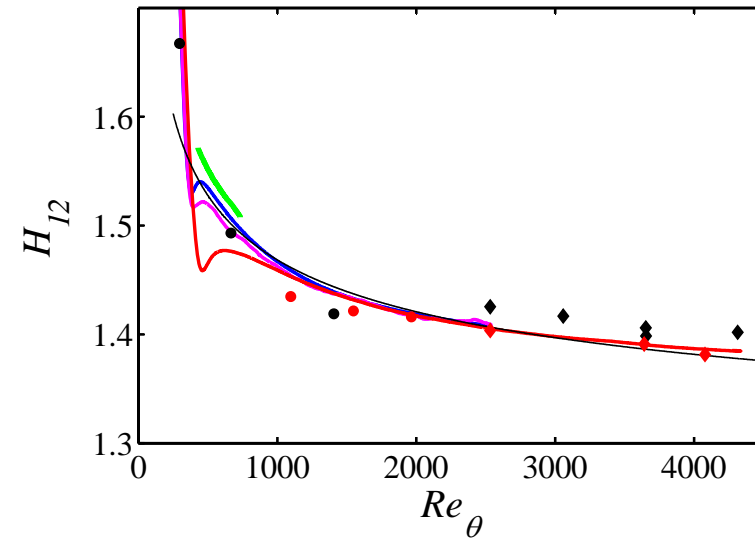
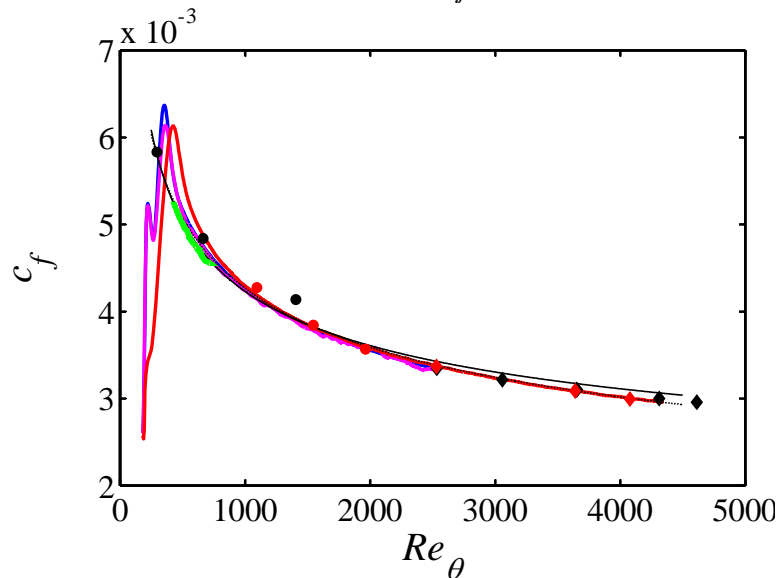


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Statistical Data

Integral Quantities up to $Re_\theta=4300$

- Skin friction c_f and shape factor H_{12}



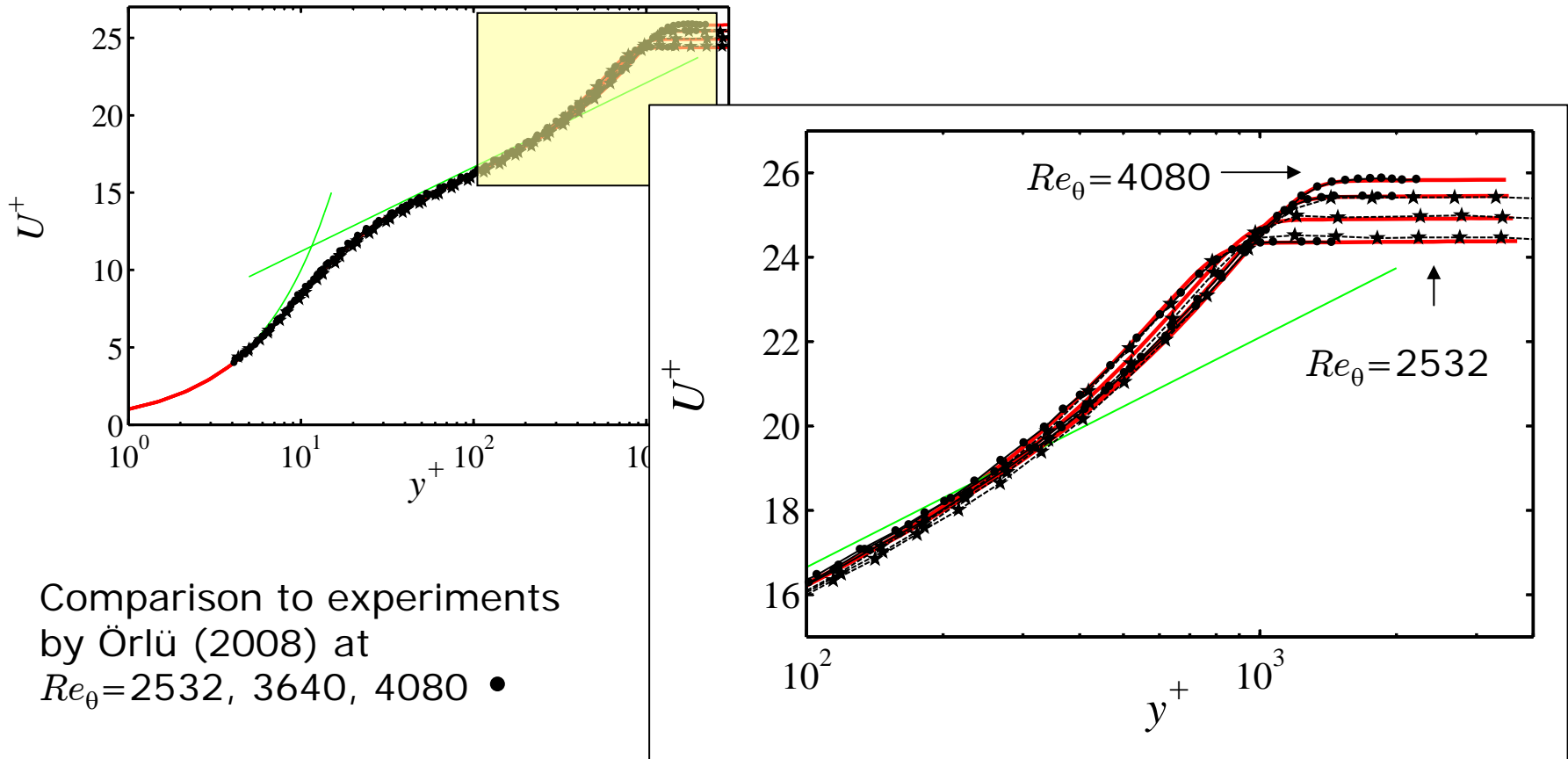
- DNS Spalart (1988) $Re_\theta=300, 670, 1410$
- DNS Jiménez et al. (2009) $Re_\theta=1100, 1550, 2000$
- EXP Österlund (1999) $Re_\theta=2500, 3000 \dots$
- EXP Örlü (2008) $Re_\theta=2500, 3000 \dots$
- Correlations (Monkewitz et al. 2007, Österlund (1999))
- DNS Skote (2001)

— Medium DNS — Fine LES — Fine DNS



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Comparison to Experiments



Comparison to experiments
by Örlü (2008) at
 $Re_\theta = 2532, 3640, 4080$ •

and Österlund (1999) at
 $Re_\theta = 2532, 3060, 3651$ ★

— present LES at matching Re_θ



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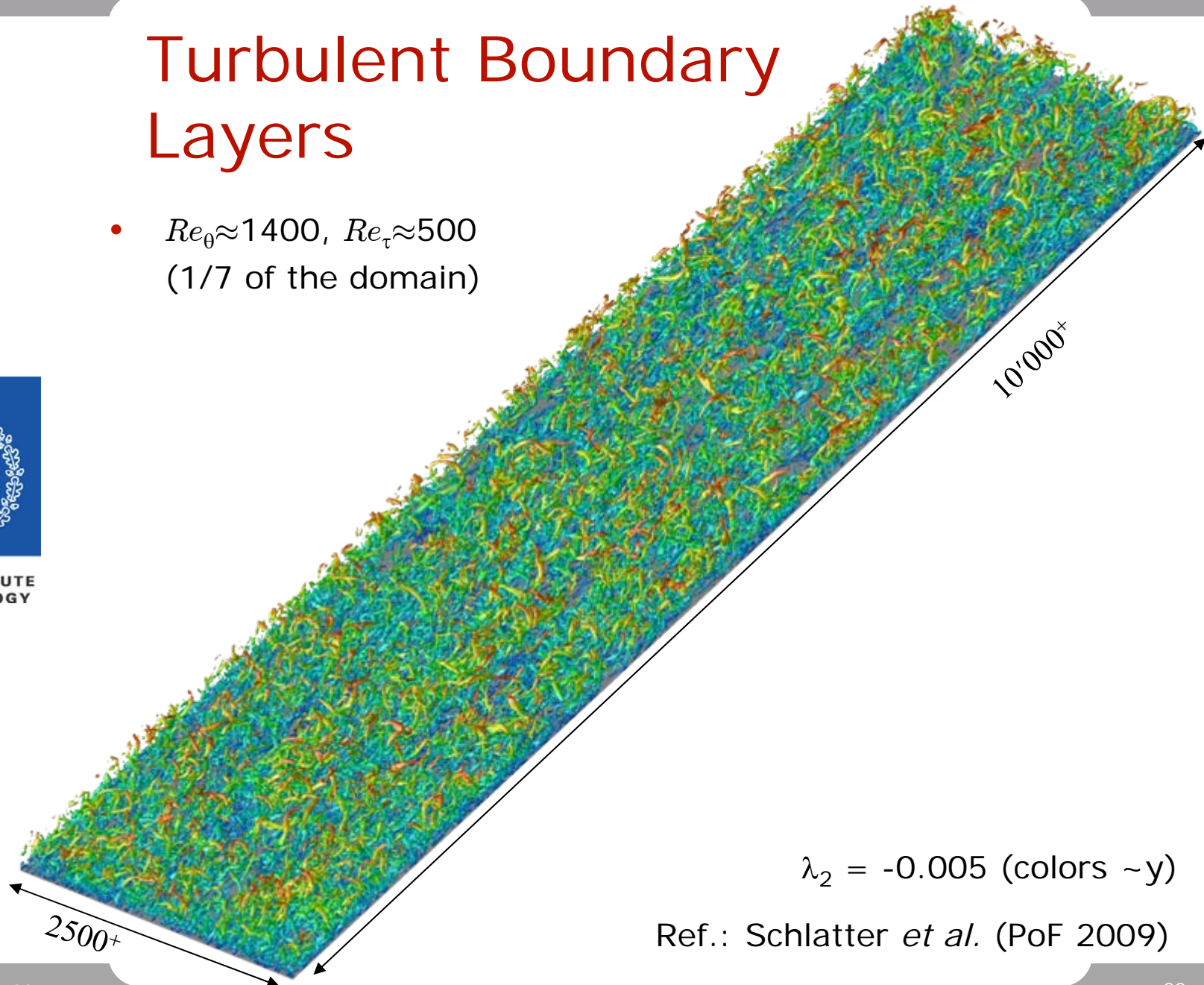
Visualisation – “Large-Scale” Structures

Turbulent Boundary Layers

- $Re_\theta \approx 1400$, $Re_\tau \approx 500$
(1/7 of the domain)



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$\lambda_2 = -0.005$ (colors $\sim y$)

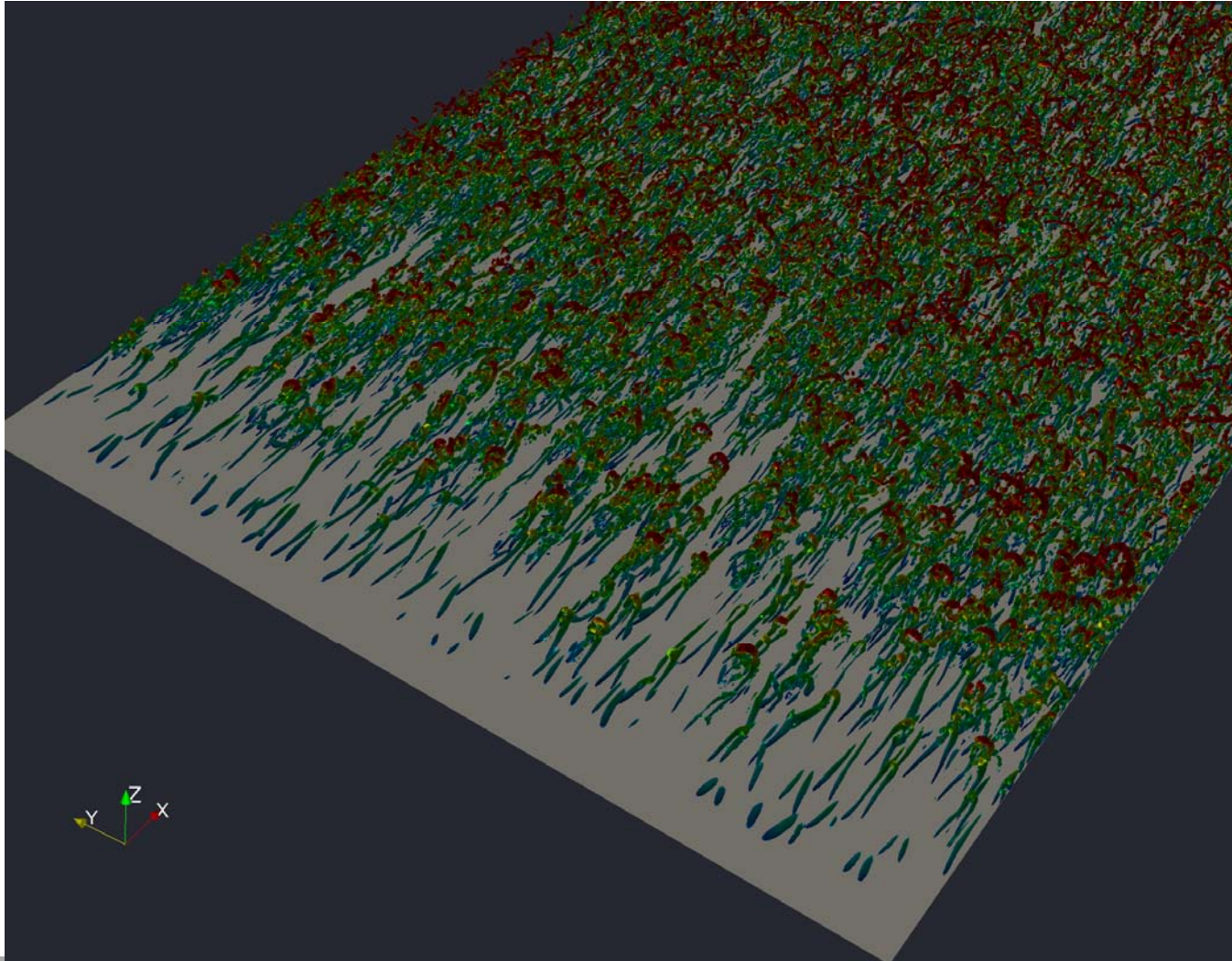
Ref.: Schlatter *et al.* (PoF 2009)

Up to $Re_\theta = 700\dots$ (DNS)



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$Q=0.015$

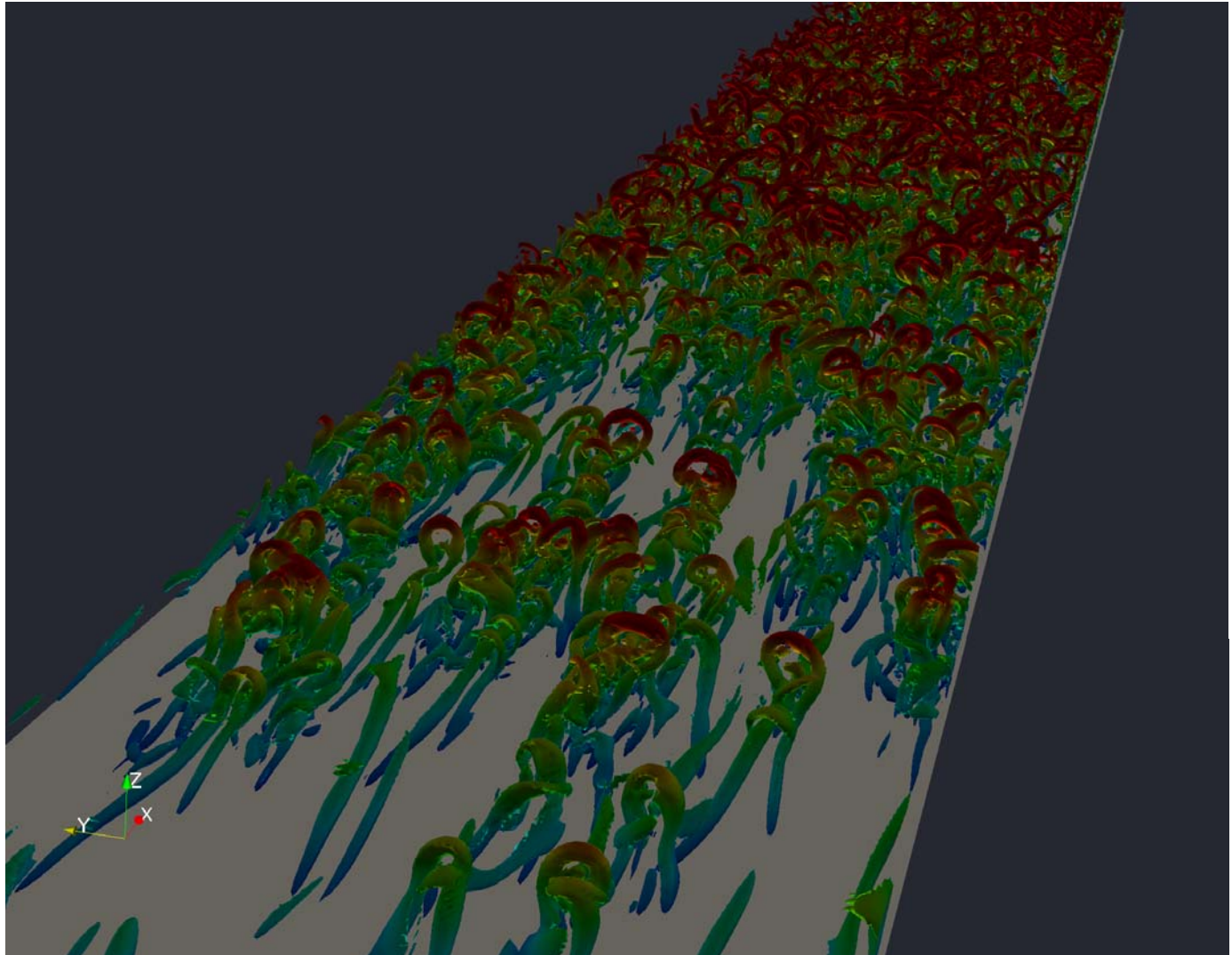
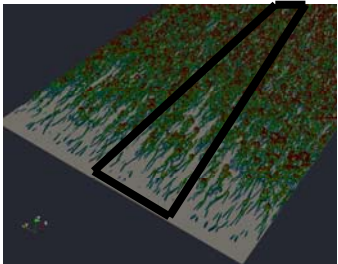


Up to $Re_\theta = 700\dots$ (DNS)



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$$Q=0.015$$



Visualisation High-Re

- Visualisation of:
 - streamwise velocity $u=0.8$
 - $\lambda_2 = -0.002, -0.005$ and -0.008
- $Re_\theta = 4000$
- real aspect ratio
- **visualised domain:**
 - 1/7 in streamwise direction
 - 1/2 in wall-normal direction
 - total $200 \cdot 10^6$ grid points

→ 7% of the computational domain

Paraview (VTK) running at PDC on $O(16)$ nodes)

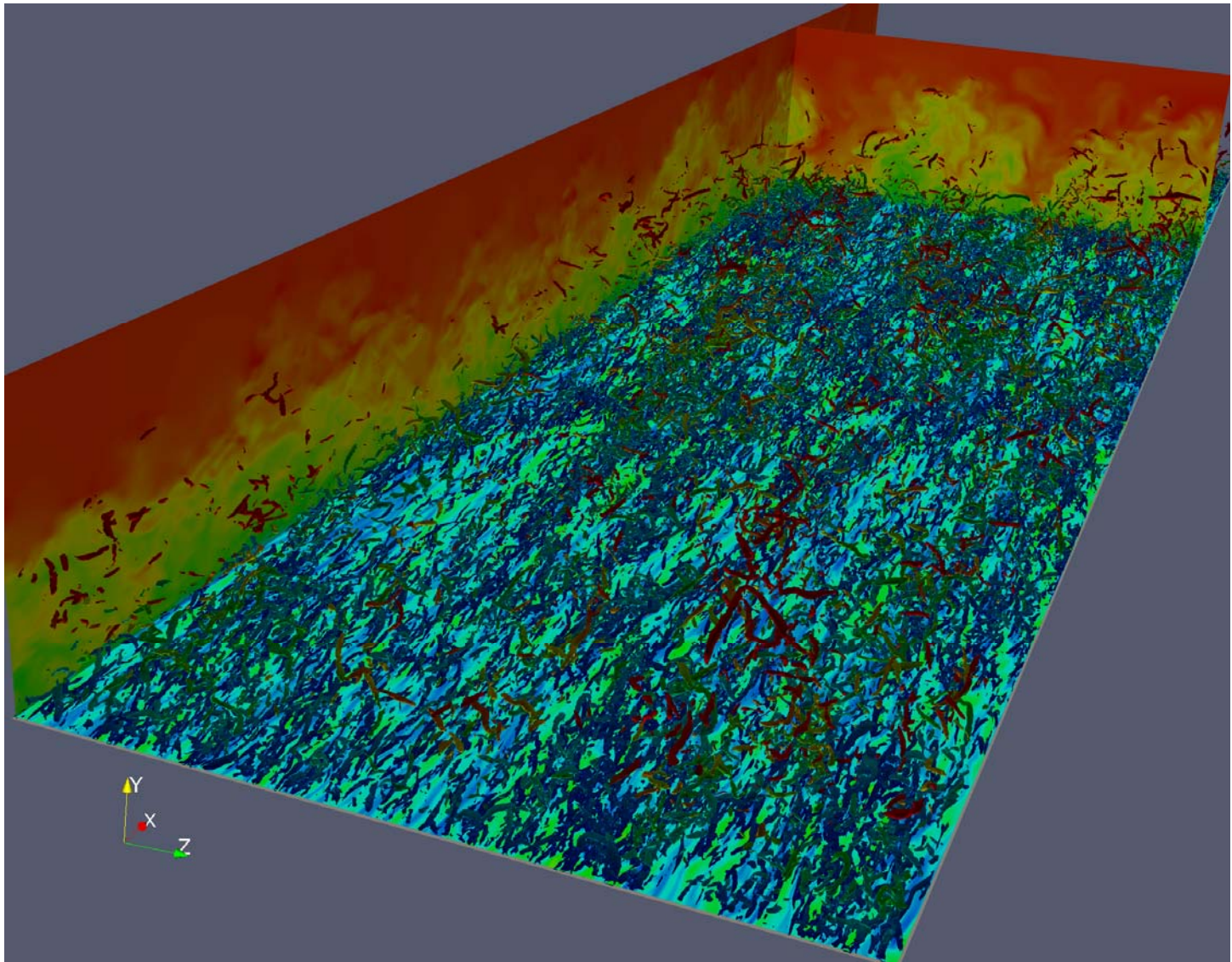


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$$Re_\theta = 4000$$



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flow
direction

$$\lambda_2 = -0.005, \text{ colour} \sim y$$

Conclusions and Outlook

- Simulation of turbulent flows is a **computationally expensive** endeavour
- Turbulence close to walls and in climate (ocean etc.) main aspects of research on **Ekman**: basic open questions, practical relevance
- DNS/LES of a **spatial turbulent zero pressure gradient turbulent boundary layer** up to $Re_0=4300$ (data: www.mech.kth.se).
→ Largest simulations to date for this geometry.
- **Ekman** (and similar machines) are a welcome and necessary complement (but not replacement) to SNIC resources.
- **Visualisation of high-Re turbulent boundary layers**: No clear hairpin vortices detected except for low-Re region.
- Outlook:
 - **Numerical/Computational Methods** as a focal area with new Swedish eScience strategy; KTH/LiU/SU/KI



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