



Delivering Interactive
Parallel Computing Power
to the Desktop

sgi[®]

An Interactive Approach to Parallel Computing Algorithms with Star-P

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Parallel Computing Arts

Message Passing:



The King's Messenger

Batch Processing: Coding, Modeling, & Debugging



Punch Cards (textile loom 1840)

Noble perfected arts: what's next for productivity?

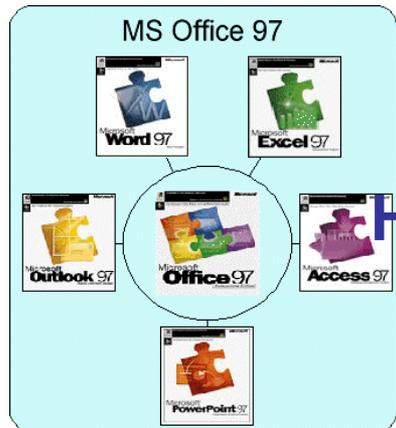
Productivity



← Make this machine go faster?

Most important catalysts for productivity are

Interactivity & ease of use

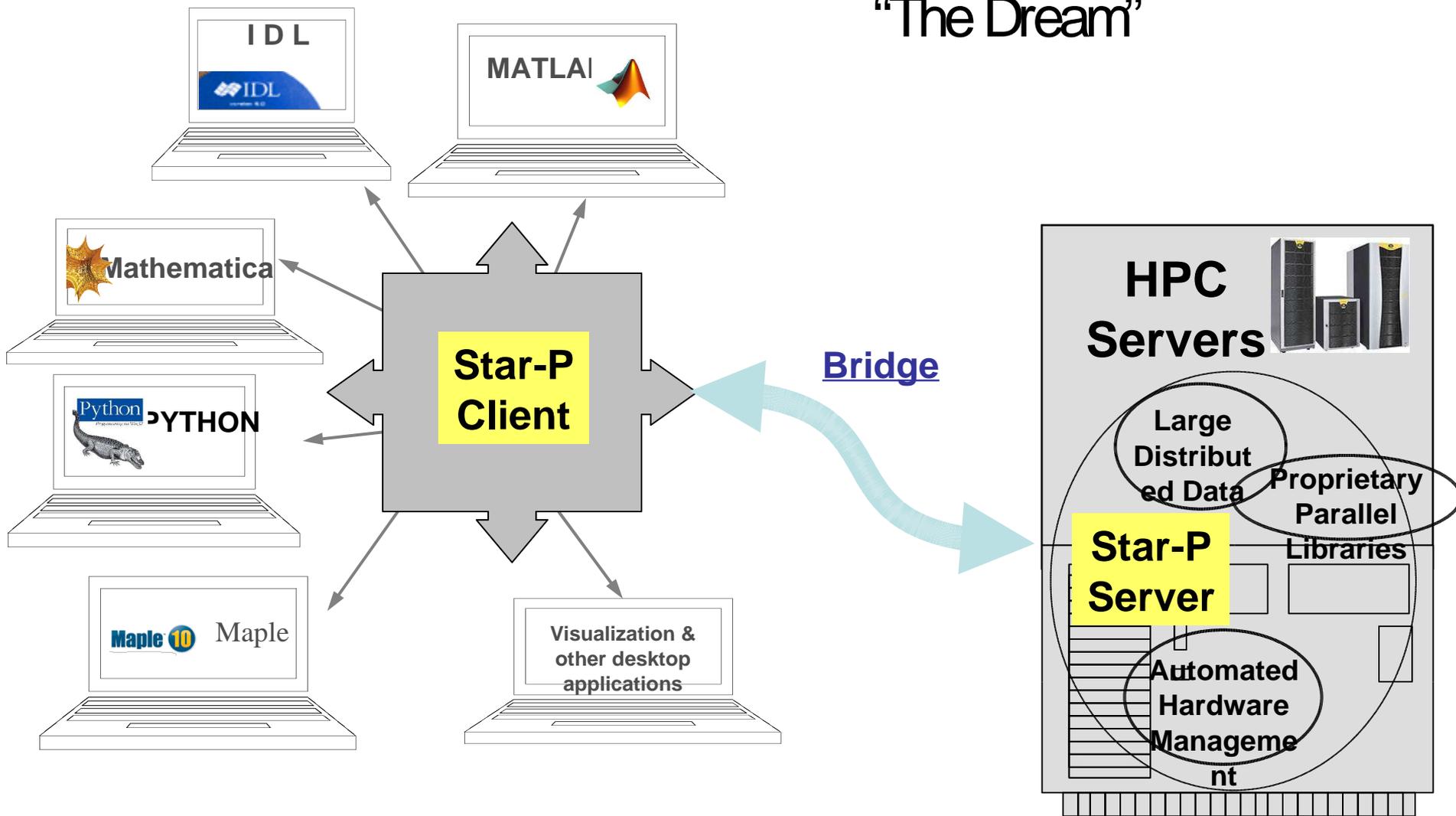


← puzzle pieces working together
Humans interacting online →



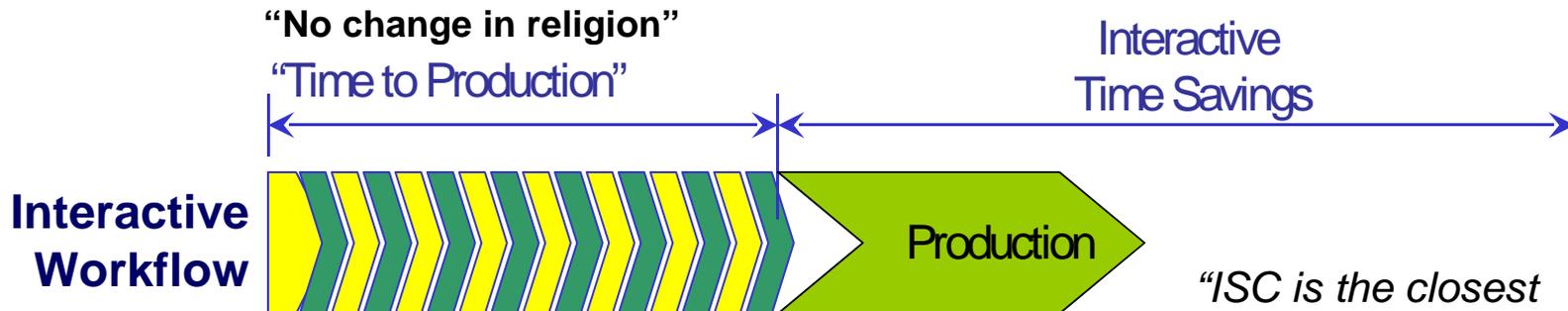
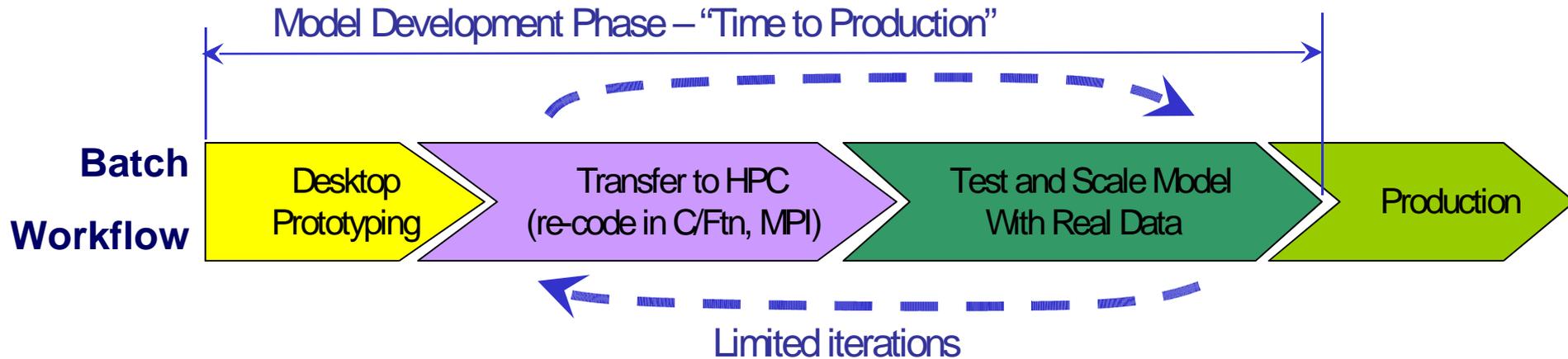
Star-P = A Software Platform For Interactive Supercomputing

“The Dream”



INTERACTIVE Fundamentally Alters the Flawed Process

Re-coding takes time, and invariably takes away from model refinement



“ISC is the closest thing I’ve seen to a killer app.”

John Mucci
CEO, SiCortex



High Productivity Design Principles

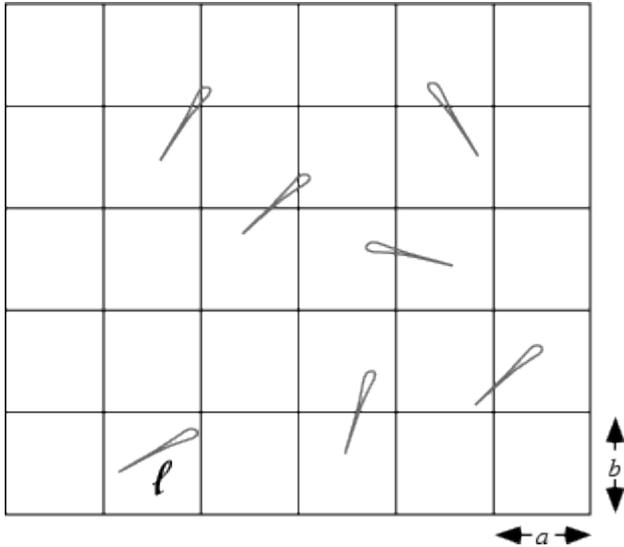
Rich set of High Performance primitives & tools.

- a. Interoperate
- b. Interactive

**OK to exploit special-purpose hardware as appropriate
(FGPGAs, GPUs)**

**Do it yourself (in MPI, OpenMP, etc.,) → do it for
everyone!**

The Buffon Needle Problem



$$P(l;a,b) = (2l(a+b) - l^2) / (\pi ab)$$

```
function z=buffon(a,b,l, trials)
```

```
%% Embarrassingly Parallel Part
```

```
r=rand(trials,3);
```

```
x =a*r(:,1)+l*cos(2*pi*r(:,3)); % x coord
```

```
y =b*r(:,2)+l*sin(2*pi*r(:,3)); % y coord
```

```
inside = (x >= 0) & (y >= 0) & (x <= a) & (y <= b);
```

```
%% Collective Operation (the sum)
```

```
bpi=(2*l*(a+b) - l^2)/(a*b*(1-sum(inside)/trials));
```

```
%% Front end
```

```
z=[buffonni:pi;abs(pi-buffonpi)/pi];
```

```
buffon(1,1,.5,10000*p)
```

Star-P Language

MATLAB™, plus

global view (v. node-oriented)

Strong bias towards propagation of distributed attribute

*p denotes dimension of distributed array

Overloading of operators

ppeval for task parallelism

Empirical data: typically have to change 10-20 SLOC for MATLAB codes to work in Star-P

xxx == explicit parallel extension

yyy == parallelism propagated implicitly

```
a = rand(n,n*p);
```

```
ppload imagedata a
```

```
[nrow ncol] = size(a);
```

```
b = ones(nrow,ncol);
```

```
c = fft2(a);
```

```
d = ifft2(c);
```

```
diff = max(max(abs(a-d)));
```

```
if (diff > 10*eps)
```

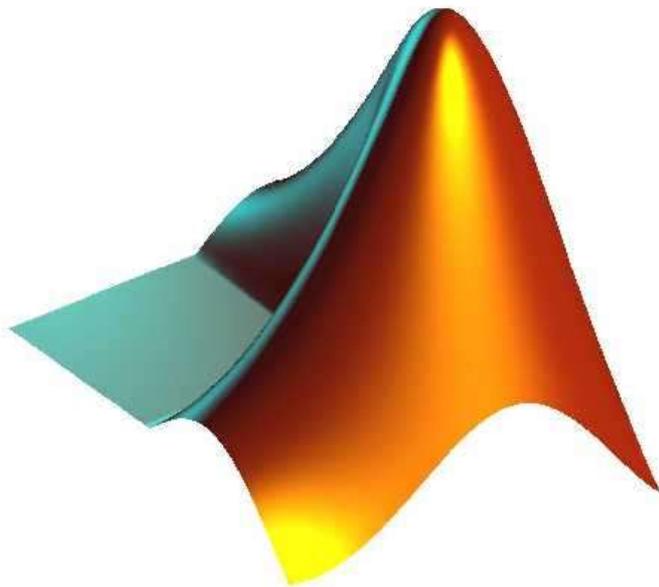
```
    sprintf('Error, diff=%f', diff);
```

```
end
```

```
e = ppeval('sum',a);
```

```
e = ppeval('quad','fun',a);
```

It's still MATLAB!



1. File Editor
2. Profiler
3. Debugger
4. Array Editor
5. Desktop
6. Viz
7. Small Calculations
8. ...

Opening Star-P



1. Windows: Hit the Little Button

2. Linux:

```
starp <options>
```

```
-a server_host
```

```
-t data_dir_on_server
```

```
-s path_to_star-p_on_server
```

```
-p number_of_processors
```

- Console mode vs desktop mode

Closing Star-P

```
>> quit
```

It's still MATLAB!

My first Star-P session

<MATLAB>

Copyright 1984-2005 The MathWorks, Inc.

Version 7.0.4.352 (R14) Service Pack 2

January 29, 2005

Connecting to Star-P Server with 4 processes

Star-P Client.

(C) MIT 2002-04.

(C) Interactive Supercomputing, LLC 2004.

All Rights Reserved.

>> 1+1

ans =

2

>> A=randh(100*p)

A =

ddense object: 100p-by-100p

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How many p's?



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served.

100x100 on the server

ans =

2

>> A=rand(100*p)

A =

ddense object: 100p-by-100p

1. **rand($10^*p, 10$)** row distributed
2. **rand($10, 10^*p$)** column distributed
3. **rand($10^*p, 10^*p$)** or **rand(10^*p)**
block cyclic distributed

1. **rand($10^*p, 10$)** row distributed
2. **rand($10, 10^*p$)** column distributed
3. **rand($10^*p, 10^*p$)** or **rand(10^*p)**
block cyclic distributed

What is this p anyway?

1. **rand(10*p,10)** row distributed
2. **rand(10,10*p)** column distributed
3. **rand(10*p,10*p)** or **rand(10*p)**
block cyclic distributed

What is this p anyway?

- World's dumbest symbolic var?
- Better to tag dimensions than arrays!

MATLAB language & experience

Minimal code changes

Server has big data

- a. Distributed attribute, once established, should be propagated
 - Operators on distributed data should preserve distribution
 - Arrays created via indexing should preserve distribution
- b. Data should be moved back to the client only as a last resort, and usually via explicit user direction
- c. Some minor behavioral changes OK, as dictated by big data

New Variables / Routines

p

“Symbolic” variable denoting distribution of array dimension

np

a. Number of processors

Small set of added commands (prefixed by “pp”)

a. ppeval (MIMD mode)

b. Data query: ppwhos

c. Data movement: ppload/ppsave, matlab2pp/pp2matlab

d. Performance monitoring: pptic/pptoc

Indexing: Examples

```
a = rand(1000*p); b = rand(1000*p);
```

```
C = a(1:end, 1:end);
```

```
D = a(18:23, 47:813);      %all distributed
```

```
E = a( : );
```

```
F = a(47,18);             % scalar -> local
```

Explicit Data Movement

pp2matlab / matlab2pp

Ideal: Never use pp2matlab

Rather use “display”

Ideal: Never use matlab2pp

Rather use “reshape”

Global Array syntax

```
aa = rand(n,n*p);           % explicitly parallel with *p
pload 'imagedata' aa      % explicitly parallel with pload

[nrow ncol] = size(aa);    % implicitly parallel
bb = ones(nrow,ncol);     % ''
cc = fft2(aa);            % ''
dd = ifft2(cc);           % ''

diff = max(max(abs(aa-dd)));
if (diff > 100*eps)
    sprintf('Numerical error in fft/ifft, diff=%f', diff);
end
```

Data Parallel vs Global Array Syntax

Usually used synonymously

Probably unfortunate:

$C=A+B$ is both

Data parallel not GAS

for $i=1:n$, for $j=1:n$

$c(i,j)=a(i,j)+b(i,j)$

end, end

Star-P aimed for big data sizes

- a. i.e., bigger than the desktop

“Vectorization” will be important

- a. Client/server architecture introduces some latency
- b. Communicating with the server in larger chunks preferred

Instrumenting Code

`pptic/pptoc`

- a. Usage like `tic/toc`
- b. Provides information about client-server traffic and server execution variables (time, counts of key operations)

PPPROFILING

```
global PPPROFILING;  PPPROFILING = 1
```

- c. Gives information about each client/server call

Large Memory Demo

```
>> np
```

```
ans =
```

```
56
```

```
>> scale
```

```
echo on
```

```
n = sqrt(0.8*m/8)
```

```
n =
```

```
5.9161e+05
```

```
aa = rand(n*p, n*p);
```

```
tic ; sum(sum(aa)), toc
```

```
ans =
```

```
1.7500e+11
```

```
Elapsed time is 260.589829 seconds.
```

```
>> whose
```

```
Your variables are:
```

Name	Size	Bytes	Class
aa	591607px591607p	2.799991e+12	ddense array
ans	1x1	8	double array
m	1x1	8	double array
n	1x1	8	double array

```
Grand total is 3.499988e+11 elements using 2.799991e+12 bytes
```

```
29MATLAB has a total of 3 elements using 24 bytes
```

pptic/pptoc Usage

```
>> a = rand(100);  
>> B = rand(100*p);  
>> % B is distributed, a is local; a will get moved  
    to the server  
>> pptic, C = a+B; pptoc;
```

Client/server communication info:

Send msgs/bytes	Recv msgs/bytes	Time spent
4e+00 / 2.080e+02B	4e+00 / 8.054e+04B	7.032e-01s

Server info:

```
execution time on server: 2.621e-02s  
#ppchangedist calls: 0
```

PPPROFILING Usage

```
>> global PPPROFILING ; PPPROFILING = 1
PPPROFILING =
    1
>> a = rand(1000*p)
ppbase_addDense    [ 2]
    [1000]
    [1000]
    [  1]
    [  1]
    [  3]
time=0.67036
a =
    ddense object: 1000p-by-1000p
>> b = fft(a)
ppfftw_fft    [1x1 com.isc.starp.ppclient.MatrixID]
    [          0]
    [          1]
time=0.30302
ppbase_id2ddata    [6]
time=0.14625
b =
```

Sparse Matrices & Combinatorial Algorithms

Combinatorial Algorithm Design Principle: Do it with a sparse matrix

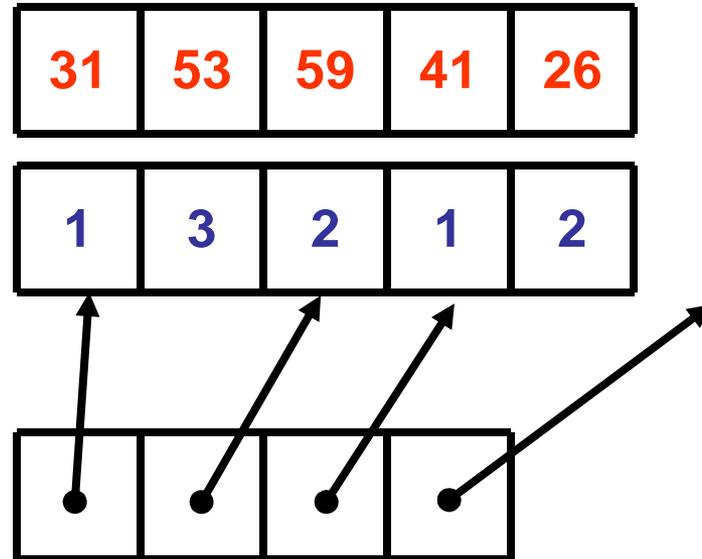
Graph Operations are well expressed with **sparse matrices** as the data structure.

Primitives for combinatorial scientific computing.

- a. Random-access indexing: `A(i, j)`
- b. Neighbor sequencing: `find (A(i, :))`
- c. Sparse table construction: `sparse (I, J, V)`
- d. Matrix * Vector: walking on the graph

Star-P sparse data structure

31	0	53
0	59	0
41	26	0



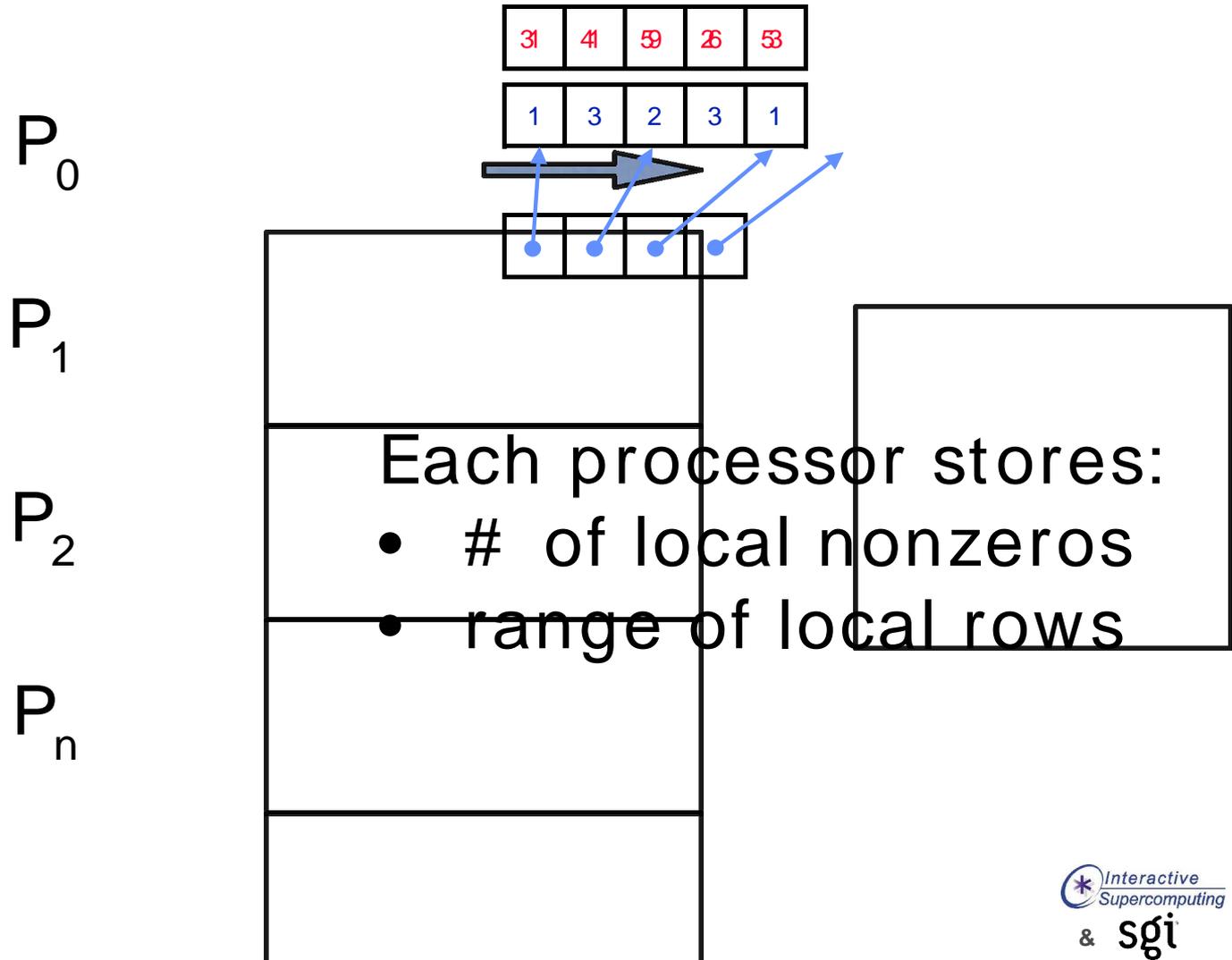
- Full:

- 2-dimensional array of real or complex numbers
- $(nrows * ncols)$ memory

- Sparse:

- compressed row storage
- about $(2 * nzs + nrows)$ memory

Star-P distributed sparse data structure



SSCA#2 Graph Theory Benchmark



High Productivity Computer Systems

**Scalable Synthetic Compact
Application (SSCA)
Benchmarks**

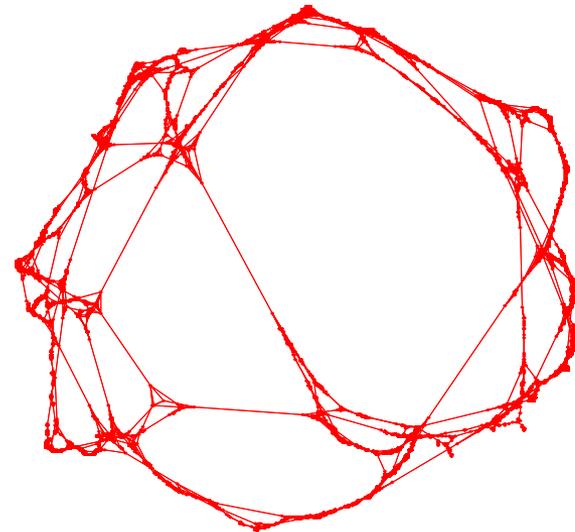
**Bioinformatics Optimal Pattern
Matching**

Graph Theory

Sensor Processing

**SSCA#2:- Graph Analysis;
stresses memory access;
compute-intensive and
hard to parallelize.**

8192-vertex graph from Kernel 1 plotted with Fiedler coordinates



Kernel 1: Construct graph data structures

Bulk of time for smaller problems

Kernel 2: Search within large sets

Kernel 3: Subgraph extraction

Kernel 4: Graph clustering

Version does not scale for larger problems

OpenMP Contest:

<http://www.openmp.org/drupal/sc05/omp-contest.htm>

3. First prize: \$1000 plus a 60GB iPod.

4. Second prize: \$500 plus a 4GB iPod nano.

5. Third prize: \$250 plus a 1GB iPod shuffle

Scalability

Kernels 1 through 3 ran on $N=2^{26}$

- Previous largest known run is $N=2^{21}$ or 32 times smaller on a Cray MTA-2
- Timings scale reasonably – we played with building the largest sparse matrix we could, until we hit machine limitations!
 - 2xProblem Size \rightarrow 2xTime
 - 2xProblem Size & 2xProcessor Size \rightarrow same time

Lines of Code

Lines of executable code (excluding I/O and graphics based on original codes available):

	cSSCA2	The spec	Pthreads
Kernel 1	29	68	256
Kernel 2	12	44	121
Kernel 3	25	91	297
Kernel 4	44	295	241

Expressive Power: SSCA#2 Kernel 3

Star-P (25 SLOC)

```
A = spones(G.edgeWeights{1});
nv = max(size(A));
npar = length(G.edgeWeights);
nstarts = length(starts);
for i = 1:nstarts
    v = starts(i);
    % x will be a vector whose nonzeros
    % are the vertices reached so far
    x = zeros(nv,1);
    x(v) = 1;
    for k = 1:pathlen
        x = A*x;
        x = (x ~= 0);
    end;
    vtxmap = find(x);
    S.edgeWeights{1} = G.edgeWeights{1}...
        (vtxmap,vtxmap);
    for j = 2:npar
        sg = G.edgeWeights{j}(vtxmap,vtxmap);
        if nnz(sg) == 0
            break;
        end;
        S.edgeWeights{j} = sg;
    end;
    S.vtxmap = vtxmap;
    subgraphs{i} = S;
end
```

MATLABmpi (91 SLOC)

```
declareGlobals;

% Wait for a response for each request we sent out.
for unused = 1:numReq
    [src tag] = probeSubgraphs(G, [P.tag.K3.dataReq];
    [starts newEdges] = MPI_Recv(src, tag, P.comm);
    subEdgeWeights{1}(:, starts) = newEdges;
    [newEnds unused] = find(newEdges);
    allNewEnds = [allNewEnds; newEnds];
end
end % of if -P.parr

% Eliminate any new ends already in the all starts list.
newStarts = setdiff(allNewEnds, allStarts);
allStarts = [allStarts; newStarts];

if ENABLE_PLOT_K3DB
    plotEdges(subEdgeWeights{1}, startVertex, endVertex, k);
end % of ENABLE_PLOT_K3DB

if isempty(newStarts) % if empty we can quit early.
    break;
end
end

% Append to array of subgraphs.
graphList = [graphList; sub];
end

function graphList = subgraphs(G, pathLength, startVPairs)

graphList = [];

% Estimated # of edges in a subgraph. Memory will grow as needed.
estNumSubGEEdges = 100; % depends on cluster size and path length

% Find subgraphs.
% Loop over vertex pairs in the starting set.
for vertexPair = startVPairs
```

	cSSCA2	executable spec	C/Pthreads/ SIMPLE
Kernel 1	29	68	256
Kernel 2	12	44	121
Kernel 3	25	91	297
Kernel 4	44	295	241

```
startDests = floor((newStarts - 1) / P.myV);
uniqDests = unique(startDests);
for dest = uniqDests
    starts = newStarts(startDests == dest);

    if dest == P.myRank
        newEdges = G.edgeWeights{1}(:, starts - P.myBase);
        subEdgeWeights{1}(:, starts) = newEdges;
        [allNewEnds unused] = find(newEdges);
        else! -isempty(starts)
```

Interactivity!

Did not just build a benchmark: Explored an algorithm space!

Spectral Partitioning based on Parpack was fine for small sizes but not larger.

We played around! We plotted data! We had a good time. 😊 Parallel computing is fun again!

Interactive Supercomputing

No “change in religion”

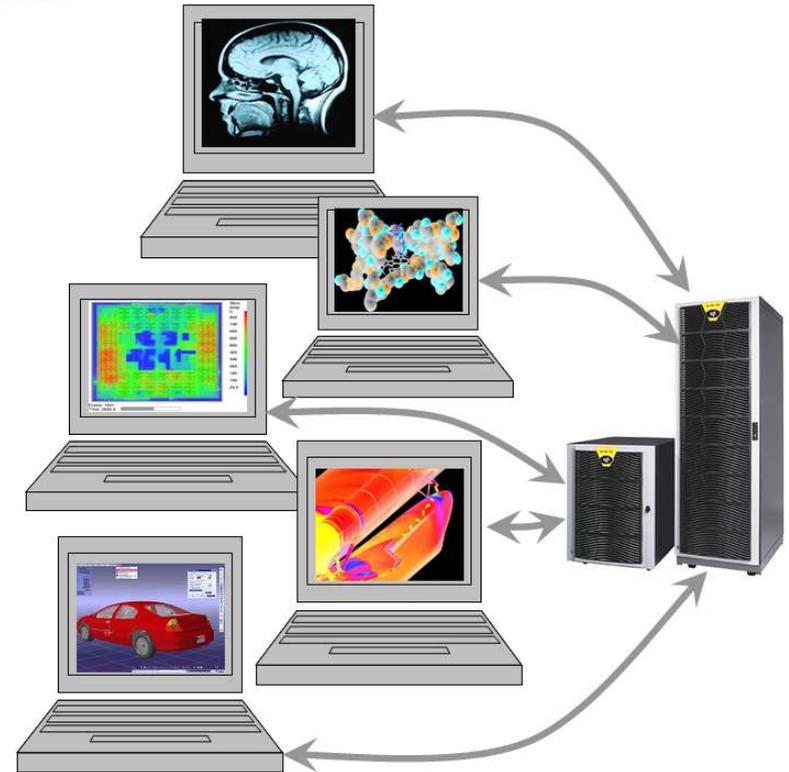
- a. Use familiar tools
- b. Desktop, interactive

5-10x manpower savings by transforming workflow

- a. Enables rapid (and more frequent) iteration
- b. Drives better conclusions, decisions, products

Improves “Time to Production”

- a. 50% reductions in calendar time
- b. Improves time to market
- c. Increases profits



"In computing with humans, response time is everything.... One's likelihood of getting the science right falls quickly as one loses the ability to steer the computation on a human time scale."

Prof. Nick Trefethen
Oxford University



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Parallel Computing Power
to the Desktop

sgi[®]

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